

A

18221

120 MINUTES

- Let a, b, c be distinct rational numbers such that $a + b + c = 0$. Then the equation $ax^2 + bx + c = 0$ has:
A) Two non real complex roots B) Two irrational roots
C) Two rational roots D) One rational root and one irrational root
- Which of the following is not true of the graph of the function $y = 3^{-x}$
A) The curve lies above the x-axis
B) The curve does not pass through the origin
C) The curve cuts one of the axis
D) The value of y increases when x increases
- The domain of the real valued function $y = \sqrt{(x - 5)(3 - x)}$ is:
A) $[-3, 5]$ B) $[-5, -3]$ C) $[3, 5]$ D) $[-5, 3]$
- The centroid of the triangle formed by the lines $x = 0, y = 0$ and $5x + 3y = 15$ is:
A) $(1, \frac{5}{3})$ B) $(\frac{5}{3}, \frac{3}{5})$ C) $(\frac{3}{5}, \frac{5}{3})$ D) $(\frac{5}{3}, 1)$
- The equation of the tangent to the parabola $y^2 - 2x - 6y + 5 = 0$ at the point $(-2, 3)$ is:
A) $x + 2 = 0$ B) $x - 2 = 0$ C) $y + 3 = 0$ D) $y - 3 = 0$
- The number of common tangents to the circles $x^2 + y^2 = 36$ and $x^2 - 6x + y^2 = 0$ is:
A) 0 B) 1 C) 2 D) 4
- If $\cos \alpha, \cos \beta, \cos \gamma$ are the direction cosines of a straight line then $\sin^2 \alpha + \sin^2 \beta + \sin^2 \gamma =$
A) 1 B) 2 C) 3 D) $\frac{1}{2}$
- The angle between the line joining $(3, 2, -2)$ and $(4, 1, -4)$ and the line joining $(4, -3, 3)$ and $(6, -2, 2)$ is:
A) $\frac{\pi}{6}$ B) $\frac{\pi}{4}$ C) $\frac{\pi}{3}$ D) $\frac{\pi}{2}$
- If the plane $2x + 3y - 5z = 0$ contains the straight line $\frac{x}{l} = \frac{y}{4} = \frac{z}{2}$ then the value of l is:
A) 1 B) -1 C) 2 D) -2

10. The function of $f(x) = e^{x-1}$ has:
 A) A local minimum at $x = 1$
 B) A local maximum at $x = 1$
 C) A local minimum at $x = 1$ and a local maximum at $x = 1$
 D) Neither local maximum nor local minimum
11. $\int_0^1 x(1-x)^{\frac{1}{2}} dx =$
 A) $\frac{3}{2}$ B) 7 C) $\frac{2}{3}$ D) $\frac{4}{15}$
12. The area bounded by the curve $y = |x + 2|$, the x -axis and the straight lines $x = 3$, $x = -3$ is
 A) 3 square units B) 5 square units
 C) 13 square units D) 21 square units
13. A fair die is thrown twice. The sum of numbers appearing is observed to be 8. The conditional probability that 3 has appeared at least once is:
 A) $\frac{2}{5}$ B) $\frac{3}{8}$ C) $\frac{5}{36}$ D) $\frac{11}{36}$
14. Let $a_n = n - n\sqrt{1 - \frac{1}{n}}$. Then $\lim_{n \rightarrow \infty} a_n =$
 A) 0 B) 1 C) $\frac{1}{2}$ D) $\frac{1}{4}$
15. The limit of the series $\sum_{n=0}^{\infty} \frac{1}{(2n)!}$
 A) e B) $e + e^2$ C) $\frac{e+e^2}{2}$ D) $\frac{e^2+1}{2e}$
16. Let $f_n(x) = \begin{cases} 1, & \text{if } -\frac{1}{n} \leq x \leq \frac{1}{n} \\ 0, & \text{otherwise.} \end{cases}$

Then which of the following is true about the sequence (f_n)

- A) $f_n(x)$ converges to 0 for all x
 B) $f_n(x)$ converges to 1 for all x
 C) $f_n(x)$ converges to 1 for all $x \in (0, 1)$
 D) $f_n(x)$ converges to 0 for all $x \in (0, 1)$
17. For the surface $z = 2x^4 + 4xy + y^2$, the origin is
 A) a saddle point B) a minimum point
 C) a maximum point D) None of these types of points

18. Let $f(x) =$ the greatest integer $< x$ and

$$g(x) = \begin{cases} 0 & \text{if } x \text{ is an integer} \\ x - f(x) & \text{otherwise} \end{cases}$$

Then which of the following is true about $f + g$.

- A) Continuous at 0 and discontinuous at 1
- B) Continuous at 1 and discontinuous at 0
- C) Continuous at 0 and discontinuous at $\frac{1}{2}$
- D) Continuous at $\frac{1}{2}$ and discontinuous at 0

19. Let f, g be functions defined on $[0, \pi]$ as follows:

$$f(x) = \begin{cases} \sin x & \text{if } 0 \leq x \leq \pi/2 \\ 0, & \text{otherwise} \end{cases}$$

$$g(x) = \begin{cases} \sin\left(\frac{1}{x}\right) & \text{if } 0 < x \leq \pi/2 \\ 0, & \text{otherwise} \end{cases}$$

Then which of the following is true.

- A) f is of bounded variation and g is not of bounded variation in $[0, \pi]$
- B) g is of bounded variation and f is not of bounded variation in $[0, \pi]$
- C) f and g are of bounded variation in $[0, \pi]$
- D) f is not of bounded variation and g is not of bounded variation in $[0, \pi]$

20. Let $f(x) = x + 1$ and $\alpha(x) = \sin x$. Then $\int_0^{\pi/2} f(x) d\alpha(x) =$

- A) 0
- B) $\frac{\pi}{2}$
- C) π
- D) 2π

21. Let $\{E_n : n \in N\}$ be a collection of Lebesgue measurable sets and let m denote Lebesgue measure. Then which of the following is not necessarily true

- A) $m(\cap_{n \in N} E_n) = \lim_{n \rightarrow \infty} m(E_n)$ if $E_{n+1} \subseteq E_n$ for all n
- B) $m(\cap_{n \in N} E_n) = m(E_1)$ if $E_n \subseteq E_{n+1}$ for all n
- C) $m(\cup_{n \in N} E_n) = \lim_{n \rightarrow \infty} m(E_n)$ if $E_n \subseteq E_{n+1}$ for all n
- D) $m(\cup_{n \in N} E_n) = m(E_1)$ if $E_{n+1} \subseteq E_n$ for all n

22. If $z = e^{1+2i}$ then $|z| =$

- A) e
- B) e^5
- C) $e^{\sqrt{5}}$
- D) $\sqrt{5}$

23. Let u_1, u_2, \dots, u_n be the n^{th} roots of unity for $n \geq 3$. Then which of the following is not necessarily true.
- A) At least one u_i is not real B) At most two roots are real
 C) At least two roots are real D) If $u_1 \neq 1$ and if u_1 is real then $u_1 = -1$.
24. If the radius of convergence of the power series $\sum \alpha_n z^n$ is 2 then the radius of convergence of $\sum \alpha_n^2 z^n$ is
- A) 1 B) 2 C) $\sqrt{2}$ D) 4
25. Which of the following function has a removable singularity at $z = 0$.
- A) $f(z) = e^{1/z}$ B) $f(z) = \sin\left(\frac{1}{z}\right)$
 C) $f(z) = \frac{\sin z}{z}$ D) $f(z) = \frac{\sin z}{z+1}$
26. Let γ be the circle $|z| = 2$. Then $\left(\frac{1}{2\pi i}\right) \int_{\gamma} \frac{e^z - 1}{z-1} dz =$
- A) 0 B) e C) $e + 1$ D) $e - 1$
27. The order of $(1, 2)$ in the group $Z_6 \oplus Z_8$ is
- A) 6 B) 8 C) 12 D) 16
28. Which of the following groups is isomorphic to $Z_{10} \oplus Z_{12}$
- A) $Z_2 \oplus Z_{60}$ B) $Z_3 \oplus Z_{40}$ C) $Z_5 \oplus Z_{24}$ D) Z_{120}
29. Let G be a group of order 49. Then
- A) G is Abelian B) G is cyclic
 C) G is non-Abelian D) $Z(G)$ has order 7
30. Let S_3 be the symmetric group on three symbols. Then the order of the commutator subgroup of S_3 is
- A) 1 B) 2 C) 3 D) 6
31. Let \mathbb{Q}^* denote the multiplicative group of non zero rationals. Let H be the subgroup generated by $\frac{1}{2}$. Then which of the following pairs of cosets are equal.
- A) $2H$ and $3H$ B) $\frac{1}{3}H$ and $\frac{2}{3}H$
 C) $\frac{1}{4}H$ and $\frac{3}{4}H$ D) $\frac{1}{5}H$ and $\frac{1}{6}H$

32. Let \mathbb{Q}^* denote the multiplicative group of non zero rationals. Let $f: \mathbb{Q}^* \rightarrow \mathbb{Q}^*$ be the homomorphism given by $f(x) = x^2$. Then the order of $\mathbb{Q}^*/\ker f$ is
 A) 1 B) 2 C) 4 D) infinite
33. Let G be a group of order 40 and H, K be subgroups of order 5 and 20 respectively. Then which of the following is true?
 A) H and K are normal subgroups of G
 B) H is a normal subgroup of G and K is not normal in G
 C) H is not normal in G and K is normal in G
 D) H is not normal in G and K is also not normal in G
34. The number of elements in the group of units of the ring Z_{50} is:
 A) 25 B) 20 C) 10 D) 5
35. The number of zeros of the polynomial $x^2 - 5x + 6$ in the ring Z_{10} is:
 A) 2 B) 3 C) 4 D) 5
36. The characteristic of the ring $Z_6 \times Z_8$ is:
 A) 6 B) 8 C) 24 D) 48
37. Which of the following is a solution for x in the congruence relation $(127)^{12} \equiv x \pmod{12}$?
 A) 1 B) 2 C) 5 D) 7
38. Let A be the set of all polynomials given by
 $A = \{x^4 + ax^3 + bx^2 + cx + 2 : a, b, c \text{ are integers}\}$. Check the validity of the following statements about A
 i. 1 is not a zero of any polynomial in A
 ii. 2 is not a zero of any polynomial in A
 iii. 3 is not a zero of any polynomial in A
 iv. 4 is not a zero of any polynomial in A
 A) i and ii only are true B) iii and iv only are true
 C) ii and iii only are true D) i and iv only are true
39. Let Z_3 be the field of integers mod 3. Let a be a zero of $x^2 + x + 2$ and $Z_a(a)$ be the Splitting field of $x^2 + x + 2$ over Z_a . Then $a^4 =$
 A) 1 B) 2 C) $1+a$ D) $1 + a^2$
40. The degree of the splitting field of $x^3 - 2$ over the rationals is:
 A) 3 B) 4 C) 5 D) 6
41. Let A be a 5×5 nilpotent matrix. Which of the following is necessarily true of A ?
 A) A is invertible
 B) 0 is the only eigen value of A
 C) At least one row of A has all entries zero
 D) All diagonal entries of A are zero

42. Let $A = (a_{ij})$, $B = (b_{ij})$, $C = (c_{ij})$ be 10×10 matrices with the following properties. $a_{11} = 1$ and $\det A = 1$, $b_{11} = 0$ and $b_{ij} = a_{ij}$ for all other (i, j) and $\det B = -1$, $c_{11} = 2$ and $c_{ij} = a_{ij}$ for all other (i, j) . Then $\det C =$
 A) 0 B) 1 C) 2 D) 3
43. Which of the following matrix is row equivalent to the 3×3 identity matrix?
 A) $\begin{bmatrix} 2 & 1 & 0 \\ 1 & 1 & 0 \\ 1 & 1 & 1 \end{bmatrix}$ B) $\begin{bmatrix} 1 & -1 & 0 \\ 0 & 1 & 0 \\ 1 & 0 & 0 \end{bmatrix}$ C) $\begin{bmatrix} 0 & 1 & 1 \\ 1 & 0 & 0 \\ 1 & 1 & 1 \end{bmatrix}$ D) $\begin{bmatrix} 1 & 2 & 1 \\ 2 & 1 & 1 \\ 3 & 3 & 2 \end{bmatrix}$
44. Let A be a 5×5 matrix of rank 4. Then the system of linear equations $AX = 0$ has
 A) Exactly one non zero solution
 B) Exactly 4 non zero solutions
 C) No non zero solutions
 D) Infinitely many non zero solutions
45. Let A be a 4×4 matrix such that $A^2 + A - I = 0$ where I is the identity matrix. Which of the following is not necessarily true?
 A) A is invertible B) $A + I$ is invertible
 C) $A^2 + I$ is invertible D) $A - I$ is invertible
46. Let $V = \mathbb{Z}_3^3$ be the 3-dimensional vector space over the field \mathbb{Z}_3 . Then which of the following is a linearly independent set in V
 A) $\{(1, 2, 0), (0, 1, 1), (1, 1, 0)\}$
 B) $\{(1, 2, 0), (1, 1, 1), (2, 0, 1)\}$
 C) $\{(1, 2, 0), (1, 0, 1), (0, 2, 2)\}$
 D) $\{(1, 2, 0), (2, 1, 2), (2, 1, 1)\}$
47. Let W be the subspace of \mathbb{R}^3 spanned by $\{(1, 2, 1), (1, 3, 1)\}$. Then which of the following is in W .
 A) $(1, 5, 2)$ B) $(2, 3, 2)$ C) $(2, 5, 3)$ D) $(3, 5, 7)$
48. Let W be the subspace of \mathbb{R}^3 spanned by $(0, 1, 1)$. Then which of the following pairs of vectors belong to the same element in the quotient space \mathbb{R}^3 / W .
 A) $(1, 2, 1)$ and $(1, 0, -1)$ B) $(1, 1, 2)$ and $(1, -1, 1)$
 C) $(1, -1, 1)$ and $(1, -2, 1)$ D) $(1, 2, -1)$ and $(1, 1, 0)$
49. Let L be the line joining $(1, 1)$ and $(2, -1)$ in the plane \mathbb{R}^2 . Then which of the following points lie on the line parallel to L and passing through the origin.
 A) $(1, 2)$ B) $(2, 1)$ C) $(-1, 1)$ D) $(-1, 2)$

50. Which of the following is a linear transformation from $\mathbb{R}^3 \rightarrow \mathbb{R}^3$.
- A) $f(x, y, z) = (x + y, x - y, xy)$
 B) $f(x, y, z) = (1 + z, 1 - x, y)$
 C) $f(x, y, z) = (2x + y, 3x + z, 2z)$
 D) $f(x, y, z) = (2x + 3y, 2x - 3y, 1)$
51. Let $f : \mathbb{R}^4 \rightarrow \mathbb{R}^4$ be defined by $f : (x, y, z, t) = (x - y, x - z, x - t, 0)$. Then dimension of null space of f is:
 A) 0 B) 1 C) 2 D) 3
52. Let $T : \mathbb{R}^4 \rightarrow \mathbb{R}^3$ be a linear transformation which is represented by the Matrix $\begin{bmatrix} 1 & 0 & 0 & 0 \\ 1 & 1 & 2 & 0 \\ 0 & 0 & 1 & 0 \end{bmatrix}$. Then which of the following is true
- A) T is one to one and onto B) T is one to one and not onto
 C) T is onto but not one to one D) T is not one to one and not onto
53. Which of the following is the minimal polynomial of the matrix $\begin{bmatrix} 1 & 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 & 0 \\ 0 & 0 & 2 & 1 & 0 \\ 0 & 0 & 0 & 2 & 0 \\ 0 & 0 & 0 & 0 & 2 \end{bmatrix}$
- A) $(x - 1)^2 (x - 2)^3$ B) $(x - 1)^2 (x - 2)^2$
 C) $(x - 1) (x - 2)^3$ D) $(x - 1) (x - 2)$
54. For which of the following values of a and b the matrix $\begin{bmatrix} a & b & 0 \\ 0 & a & 0 \\ 0 & 0 & b \end{bmatrix}$ is diagonalizable.
- A) $a = 0, b = 1$ B) $a = 1, b = 1$
 C) $a = 1, b = -1$ D) $a = 0, b = 0$
55. The GCD of the numbers $2^7 \times 3^5 \times 5^6 \times 13^3$ and $2^5 \times 3^7 \times 5^3 \times 13^6$ is
 A) 390 B) $6^4 \times 65^3$ C) $6^5 \times 65^3$ D) $6^7 \times 65^6$
56. Let ϕ denote the Euler totient function. Then $\phi(1024) =$
 A) 1023 B) 512 C) 256 D) 64
57. Which of the following is true?
 A) $2^{12} \equiv 1 \pmod{21}$ B) $2^{12} \equiv -1 \pmod{21}$
 C) $2^{10} \equiv -1 \pmod{21}$ D) $2^{10} \equiv 1 \pmod{21}$

58. The system of equations $2x \equiv 3 \pmod{5}$ and $3x \equiv 4 \pmod{7}$ has
 A) No solution
 B) Exactly one solution ($\pmod{35}$)
 C) Exactly two solutions ($\pmod{35}$)
 D) Exactly six solutions ($\pmod{35}$)
59. Which of the following is the differential equation of the family of curves $y^2 = 4c(x + c)$
 A) $y = 2x \frac{dy}{dx} + y \left(\frac{dy}{dx}\right)^2$ B) $y = 2x \frac{dy}{dx} - y \left(\frac{dy}{dx}\right)^2$
 C) $y = 2x \frac{dy}{dx} + y^2 \left(\frac{dy}{dx}\right)^2$ D) $y = 2x \frac{dy}{dx} - y^2 \left(\frac{dy}{dx}\right)^2$
60. The solution of the differential equation:
 $\cos(x - y) dx = x \sin(x - y) dy - x \sin(x - y) dx$ is
 A) $x \sin(x - y) + \cos(x - y) = c$
 B) $x \sin(x - y) - \cos(x - y) = c$
 C) $x \sin(x - y) = c$
 D) $x \cos(x - y) = c$
61. The Wronskian of the solutions of the equation $y'' - y = 0$ is
 A) $2e^{2x}$ B) $2e^{-2x}$ C) -2 D) 2
62. The Bessel function $J_{-2}(x) =$
 A) $-J_2(x)$ B) $-2J_0(x)$ C) $J_2(-x)$ D) $J_2(x)$
63. The number of regular singular points of the function:
 $(x^3 + x^2 - 6x) \frac{d^2y}{dx^2} + x^2 \frac{dy}{dx} + (x - 2)y = 0$ is
 A) 0 B) 1 C) 2 D) 3
64. The integral of the equation $y dx - z dx + dy - dx = 0$ is
 A) $y - z = ce^x$ B) $y - z = ce^{-x}$
 C) $y + z = ce^x$ D) $y + z = ce^{-x}$
65. If $\sin^2 x u_{xz} + A u_{xy} + \cos^2 x u_{yy} = u_z$ is parabolic then the value of A is
 A) $\sin 2x$ B) $\cos 2x$ C) $2 \sin x$ D) $2 \cos x$
66. The complete integral of the equation:
 $pqz = p^2(xq - p) + q^2(yq - q)$ is
 A) $z = ax + by + \frac{1}{ab}(a^3 + b^3)$ B) $z = ax + by - \frac{1}{ab}(a^3 + b^3)$
 C) $z = ax + by - \frac{a+b}{ab}$ D) $z = ax + by + \frac{a+b}{ab}$

67. Which of the following is not a metric on \mathbb{R}^2 . Here $x = (x_1, x_2)$ and $y = (y_1, y_2)$.
- A) $d(x, y) = |x_1 - y_1| + |x_2 - y_2|$
- B) $d(x, y) = (x_1 - y_1)^2 + (x_2 - y_2)^2$
- C) $d(x, y) = \sqrt{(x_1 - y_1)^2 + (x_2 - y_2)^2}$
- D) $d(x, y) = \max\{|x_1 - y_1|, |x_2 - y_2|\}$
68. Let $X = \{1, 2, 3, 4, 5\}$ and τ_1, τ_2, τ_3 be topologies on X given as follows.
 $\tau_1 = \{X, \emptyset, \{1, 2\}\}$, $\tau_2 = \{X, \emptyset, \{1\}, \{1, 2\}\}$ and τ_3 is the discrete topology.
 Then which of the following is true
- A) τ_1 and τ_2 are metrizable
- B) τ_2 and τ_3 are metrizable
- C) τ_1 is metrizable and τ_2 is not metrizable
- D) τ_2 is not metrizable and τ_3 is metrizable
69. Let \mathbb{R} be the space of all reals with discrete topology. Let \mathbb{R}^+ be the subspace of all positive reals and \mathbb{Q}^+ be the subspace of all positive rationals. Then which of the following is true
- A) The closure of \mathbb{Q}^+ in \mathbb{R} is \mathbb{R}^+
- B) The closure of \mathbb{R}^+ in \mathbb{R} is $\mathbb{R}^+ \cup \{0\}$
- C) The interior of \mathbb{Q}^+ in \mathbb{R} is \mathbb{Q}^+
- D) The interior of \mathbb{R}^+ in \mathbb{R} is \mathbb{Q}^+
70. Let X be the space of all continuous real valued functions on $[0, 1]$ with metric given by
 $d(f, g) = \sup |f(x) - g(x)|$. Let
- $$\alpha(x) = \begin{cases} x^2: 0 \leq x \leq 1/2 \\ \frac{1}{4}: 1/2 \leq x \leq 1 \end{cases} \quad \text{and} \quad \beta(x) = \begin{cases} \frac{1}{4}: 0 \leq x \leq 1/2 \\ x^2: 1/2 \leq x \leq 1 \end{cases}$$
- Then $d(\alpha, \beta) =$
- A) 0 B) 1 C) $\frac{1}{4}$ D) $\frac{3}{4}$
71. Let τ be the topology on the reals \mathbb{R} for which $\{(-\infty, a) : a > 0\}$ is a base. Let $(a_n), (b_n)$ be sequences where $a_n = (-1)^n$ and $b_n = (-1)^n + 1$. Then which of the following is true in (X, τ) .
- A) (a_n) converges to 1 and (b_n) converges to 2
- B) (a_n) converges to -1 and (b_n) converges to 2
- C) (a_n) converges to 1 and (b_n) converges to 0
- D) (a_n) converges to -1 and (b_n) converges to 0

72. Let \mathbb{R} be the real line and \mathbb{Q} be the subspace of rationals. Then which of the following is true about a continuous function $f : \mathbb{R} \rightarrow \mathbb{Q}$
- A) f can be both one to one and onto
 B) f can be one to one and not onto
 C) f can be onto but not one to one
 D) f can not be one to one and can not be onto
73. Let X be the real line with usual topology and $Y = \mathbb{R}$ with discrete topology. Which of the following $f : X \times Y \rightarrow X \times Y$ is continuous?
- A) $f(x, y) = (x + y, x + y)$
 B) $f(x, y) = (x + y, y)$
 C) $f(x, y) = (x + 1, x)$
 D) $f(x, y) = (x, x + 1)$
74. Let $e = (1, 1, 1, \dots)$ and $f = (1, \frac{1}{2}, \frac{1}{3}, \dots)$ be sequences. With the usual notations which of the following is true.
- A) $e \in l^1$ and $f \in l^1$ B) $e \in l^1$ and $f \in l^\infty$
 C) $e \in l^\infty$ and $f \in l^2$ D) $e \in l^\infty$ and $f \in l^1$
75. Let X be the normal linear space \mathbb{R}^3 with norm $\| \cdot \|_2$ and $Y = \{ (0, y, z) : y, z \in \mathbb{R} \}$. Let $F : X/Y \rightarrow X$ be defined by $F((x, y, z) + Y) = (x, 0, 0)$. Then $\| F \| =$
- A) 0 B) 1 C) 2 D) $\frac{1}{2}$
76. Let $X = C^3$ be the normed linear space with norm $\| \cdot \|_2$. Let $F : X \rightarrow X$ be defined by $F(x, y, z) = (x, x + y, x + y + z)$. Then which of the following is not true.
- A) F is closed and continuous but not open
 B) F is closed and open but not continuous
 C) F is closed, continuous and open
 D) F is closed but not continuous and not open
77. Let X be the Hilbert space \mathbb{R}^2 . Then the set orthogonal to the point $(1, 1)$ in \mathbb{R}^2 is:
- A) The set of points on the straight lines $x = 0$ and $y = 0$.
 B) The set of points on the straight lines $x + y = 0$.
 C) The set of points on the straight lines $x - y = 0$.
 D) The set of points on the straight lines $x - y = 1$.
78. Let H be the Hilbert space and $x, y \in H$ be such that $\| x \| = 7$ and $\| y \| = 1$ and $\| x + y \| = 8$. Then $\| x - y \| =$
- A) 6 B) 5 C) 4 D) $\sqrt{2}$

79. Let $H = l^2$ be the complex Hilbert space and f be the linear functional defined by $f(x(1), x(2), \dots) = ix(1) - x(2)$. Let $e_n = (0, 0, \dots, 0, 1, 0, \dots)$ where 1 occurs in the n^{th} position. Then which of the following is true.
- A) $\sum_{n=1}^{\infty} |f(e_n)|^2 \leq \sqrt{2}$ B) $\sum_{n=1}^{\infty} |f(e_n)|^2 \leq 2$
- C) $\sum_{n=1}^{\infty} |f(e_n)|^2 \leq 1$ D) $\sum_{n=1}^{\infty} |f(e_n)|^2 \leq \frac{1}{2}$
80. Let H be the complex Hilbert space C^3 and the operator T on H be represented by the matrix $\begin{bmatrix} 1 & 0 & 0 \\ 0 & i & 0 \\ 0 & 0 & -1 \end{bmatrix}$. Then which of the following is true.
- A) T is self adjoint and unitary
 B) T is not self adjoint and not unitary
 C) T is self adjoint but not unitary
 D) T is unitary but not self adjoint
-